

$$s(t) = \sin t \text{ pro } t \in (0; \pi)$$

$$a_0 = \frac{1}{\pi} \cdot \int_0^{\pi} \sin t \cdot dt = \frac{1}{\pi} \cdot [-\cos t]_0^{\pi} = \frac{1}{\pi} \cdot (1 + 2) = \frac{2}{\pi}$$

$$\begin{aligned}
 a_n &= \frac{1}{\pi} \cdot \int_0^{\pi} \overbrace{\sin t}^u \cdot \overbrace{\cos(n \cdot t)}^{v'} \cdot dt = \frac{1}{\pi} \left\{ \frac{1}{\pi} \cdot \underbrace{[\sin(t) \cdot \sin(n \cdot t)]_0^{\pi}}_{=0} - \frac{1}{n} \cdot \int_0^{\pi} \overbrace{\cos t}^u \cdot \overbrace{\sin(n \cdot t)}^{v'} \cdot dt \right\} = \\
 &= -\frac{1}{\pi \cdot n} \left\{ -\frac{1}{n} \cdot [\cos t \cdot \cos(n \cdot t)]_0^{\pi} - \frac{1}{n} \cdot \int_0^{\pi} \sin t \cdot \cos(n \cdot t) \cdot dt \right\} = \\
 &= \frac{1}{\pi \cdot n^2} \left\{ (-1)^{n+1} - 1 + \int_0^{\pi} \sin t \cdot \cos(n \cdot t) \cdot dt \right\}
 \end{aligned}$$

$$I = \int_0^{\pi} \sin t \cdot \cos(n \cdot t) \cdot dt$$

$$I = \frac{1}{n^2} \cdot \{(-1)^{n+1} - 1 + I\}$$

$$I = \frac{(-1)^{n+1} - 1}{n^2} + \frac{1}{n^2} \cdot I$$

$$I - \frac{1}{n^2} \cdot I = \frac{(-1)^{n+1} - 1}{n^2}$$

$$I \cdot \left(1 - \frac{1}{n^2}\right) = \frac{(-1)^{n+1} - 1}{n^2}$$

$$I = \frac{\frac{(-1)^{n+1} - 1}{n^2}}{1 - \frac{1}{n^2}}$$

$$a_n = \frac{1}{\pi} \cdot \int_0^{\pi} \sin t \cdot \cos(n \cdot t) \cdot dt = \frac{1}{\pi} \cdot I = \frac{1}{\pi} \cdot \frac{(-1)^{n+1} - 1}{1 - \frac{1}{n^2}} \quad \begin{array}{l} \text{pro } n \text{ liché } a_n = 0 \\ \text{pro } n \text{ sudé } a_n = \frac{1}{\pi} \cdot \frac{-\frac{2}{n^2}}{1 - \frac{1}{n^2}} \end{array}$$

$$b_n = \frac{1}{\pi} \cdot \int_0^{\pi} \sin t \cdot \sin(n \cdot t) \cdot dt = \frac{1}{\pi} \cdot \int_0^{\pi} \frac{1}{2} \cdot [\cos(t - n \cdot t) - \cos(t + n \cdot t)] \cdot dt =$$

$$= \frac{1}{2 \cdot \pi} \cdot \int_0^{\pi} [\cos(t - n \cdot t) - \cos(t + n \cdot t)] \cdot dt$$

$$b_0 = \frac{1}{2 \cdot \pi} \cdot \int_0^{\pi} (\cos t - \cos t) \cdot dt = 0$$

$$b_1 = \frac{1}{2 \cdot \pi} \cdot \int_0^{\pi} \left[ \underbrace{\cos(t - t)}_{=1} - \cos(t + t) \right] = \frac{1}{2 \cdot \pi} \cdot \int_0^{\pi} [1 - \cos(2 \cdot t)] \cdot dt =$$

$$= \frac{1}{2 \cdot \pi} \cdot \left[ t - \frac{\sin(2 \cdot t)}{2} \right]_0^{\pi} = \frac{1}{2 \cdot \pi} \cdot (\pi - 0 - 0 + 0) = \frac{1}{2}$$

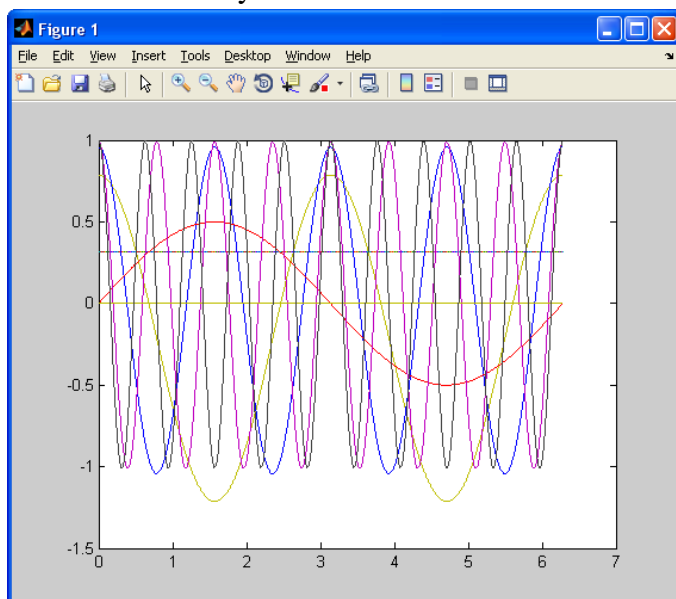
$$b_2 = \frac{1}{2 \cdot \pi} \cdot \int_0^{\pi} [\cos(t - 2 \cdot t) - \cos(t + 2 \cdot t)] \cdot dt = \frac{1}{2 \cdot \pi} \cdot \int_0^{\pi} [\cos(-t) - \cos(3 \cdot t)] \cdot dt =$$

$$= \frac{1}{2 \cdot \pi} \cdot \left[ \frac{\sin(-t)}{-1} - \frac{\sin(3 \cdot t)}{3} \right]_0^{\pi} = 0$$

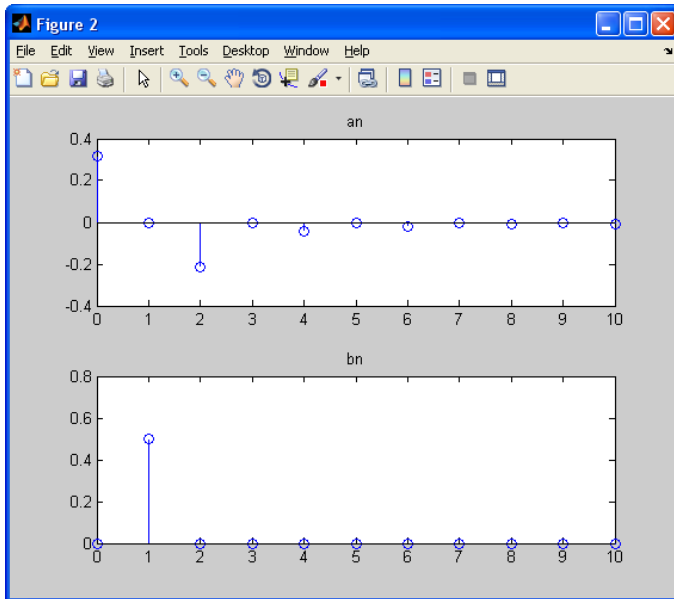
$$b_3 = 0 \dots b_{\infty} = 0$$

**Pro n = 10:**

Harmonické složky:



Velikosti složek  $a_n$  a  $b_n$ :



Výsledný průběh:

